FM DEMODULATION USING A DIGITAL RADIO AND DIGITAL SIGNAL PROCESSING

By

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by

James Michael Shima

To my mother, Roslyn Szego,

and

To the memory of my grandmother, Evelyn Richmond.

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Abstract of Thesis Presented to the Graduate School of the University of Florida in Partial Fulfillment of the Requirements for the Degree of Master of Science

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Frequency modulation (FM) and demodulation techniques are well established and understood when implemented with analog circuits. Recently, state-of-the-art digital technology allows radio-frequency (RF) signals to be processed in the discrete-time domain. Modulated RF signals are digitally sampled and then demodulated in real time using signal processing techniques and a digital signal processor (DSP). A digital board capable of these tasks is often termed a "digital radio." This paper results from the availability of a digital radio board. The flexibility of DSP software allows a realization of different demodulation schemes. The purpose of this paper was to test this new technology by implementing an FM demodulator using the digital radio. A mathematical algorithm was developed and translated into DSP software to implement the "digital FM demodulator." The testing of the digital FM demodulator provided a performance analysis of the developed algorithm. This paper addresses the detailed background, development, and testing of a digital FM demodulator as implemented on a digital radio board.

CHAPTER 1 INTRODUCTION

1.1 Background Overview

The breakthrough of high-speed digital signal processors (DSPs) have allowed traditional analog systems to be realized with today's digital circuit technology. The advances in computer technology has bred a new realm of discrete-time computing capability. The decrease in chip area and increase in transistor density of computer CPUs and DSPs have paved the way for the digital implementation of high-speed real-time systems.

DSPs have become more popular and cost effective since their inception in the early 1980s. Therefore, the low-cost DSP is able to take the place of the traditional microcontroller, unveiling more computing power and versatility at the same cost. The DSP is considered a "specialized" microprocessor, able to perform signal-processing tasks efficiently. Since most signal processing stems from the implementation of discrete-time convolution, DSPs consequently have a very fast multiply-accumulate architecture. DSPs generally execute one instruction per clock cycle and embody a Harvard-type architecture.

Analog communication systems have been around for decades. In 1918 Edwin H. Armstrong invented the superheterodyne receiver circuit, and in 1933 he also invented the concept of frequency modulation (FM). Until recently, analog receivers and modulation techniques have been unsurpassed in performance. However, new technologies in digital communications are utilized in developing high-speed modems, spread-spectrum systems,

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next-generation cellular radios, and many other digital systems that dwarf their analog counterparts.

1.2 Design Motivation

Communication systems have traditionally used all analog circuits to recover modulated radio-frequency (RF) signals. Specifically, FM is a type of analog modulation that requires an analog phase-locked loop (PLL) or slope detector for demodulation. FM and other demodulation techniques are well established and understood when implemented with analog circuits. Recently, state-of-the-art digital technology allows RF signals to be processed in the discrete-time domain. Hence, modulated RF signals are digitally sampled and then demodulated in real time using signal processing techniques and a DSP. A digital board capable of these tasks is often termed a "digital radio". The digital radio is the digital counterpart of an analog superheterodyne receiver.

The motivation of this paper stems from the availability of a state-of-the-art digital radio board. Using the power and flexibility of the digital radio board, traditional analog demodulators can be implemented in DSP software. Since DSP software can be easily changed, several "digital demodulators" can be written to implement different demodulation schemes, such as FM, amplitude modulation (AM), or single-sideband modulation (SSB). The key point of interchangeable software demonstrates the tremendous flexibility advantage a digital radio solution has over a single-task analog receiver.

The advent of digital RF technology enables numerous analog systems to be converted into one digital radio solution through the use of real-time signal processing software. Many large analog receivers can be replaced with one small digital board. Custom demodulators are also easily implemented with the digital radio because of its generic hardware architecture.

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The digital radio is in its research stage, and it has limited real-time demodulation abilities. The first step chosen to test this new technology is to implement an FM demodulator using the digital radio. FM is well established and is the backbone for many other digital communication schemes, including the frequency-shift keying (FSK) modulation family and the multilevel signaling modulation schemes. A digital FM demodulator provides a performance test for the digital radio. These test results provide some insight for the probable improvements to the digital radio architecture. Consequently, this paper addresses the background, development, and testing of a digital FM demodulator as implemented on a digital radio board.

CHAPTER 2 CONVENTIONAL AND COMPLEX ANALOG FM DEMODULATION

This chapter reviews FM communications and conventional analog FM demodulation in order to provide the theoretical framework necessary to develop a digital FM demodulator.

2.1 Frequency Modulation and the FM Equation

Frequency modulation (FM) is a type of angle-modulated signal. A conventional angle-modulated signal is defined by the following equation.

$$X_{Angle}(t) \stackrel{\Delta}{=} \mathbf{A}_{c} \cos(w_{c}t + \mathbf{P}(t))$$
(2.1)

where w_c = the carrier frequency (rad/s) A_c = constant amplitude factor P(t) = the modulating input signal m(t) = the original message signal

For FM, the relation of m(t) to P(t) is given by

$$P(t)_{FM} = D_f \cdot \int_{-\infty}^t m(\xi) \, d\xi \tag{2.2}$$

where D_f is a constant measured in radians/volt-seconds.

Taking the time derivative of both sides of Equation (2.2), it is readily seen that the message m(t) is the derivative of the modulating signal $P(t)_{FM}$. Equation (2.4) results from applying Leibniz's rule to Equation (2.3).

$$\frac{\partial}{\partial t} \left[P(t)_{FM} \right] = D_f \cdot \frac{\partial}{\partial t} \left[\int_{-\infty}^{t} m(\xi) \, d\xi \right]$$
(2.3)

$$\frac{\partial P(t)_{FM}}{\partial t} = D_f \cdot m(t)$$
(2.4)

By observing Equation (2.4), it can be seen that the instantaneous phase of an FM signal is directly related to the message m(t). The FM equation now takes the following form:

$$X_{FM}(t) \stackrel{\Delta}{=} A_{c} \cos(w_{c}t + P(t)_{FM}) = A_{c} \cos(w_{c}t + D_{f} \int_{-\infty}^{t} m(\xi) d\xi) \quad (2.5)$$

The instantaneous frequency of the FM signal in Equation (2.5) is

$$W_c + \frac{\partial P(t)_{FM}}{\partial t} = W_c + D_f m(t)$$
(2.6)

Equation (2.6) reveals that the instantaneous frequency of an FM signal varies about the carrier frequency w_c directly proportional to the message signal m(t) [Cou90]. If m(t) is a sinusoid, then the amplitude and frequency of the message determines the frequency of the cosine carrier function.

The amount of deviation from the assigned carrier frequency w_c is called the frequency deviation, or ΔF . The frequency deviation is also related to the message m(t) by the equation

$$\Delta F = \frac{1}{2\pi} \left[\frac{\partial P(t)_{FM}}{\partial t} \right]$$
(2.7)

Note that ΔF is a non-negative number measured in Hertz. The maximum frequency deviation of an FM signal, denoted ΔF_{max} , is directly proportional to the amplitude of the input signal. The equation for maximum frequency deviation is given below.

$$\Delta F_{\max} = \frac{1}{2\pi} D_f \cdot \max[m(t)]$$
(2.8)

Equation (2.8) makes it obvious that an increase in the message m(t) amplitude creates an increase in the maximum frequency deviation. The increase in frequency deviation also increases the bandwidth of the FM signal.

The important relationship established above is that the instantaneous frequency of an FM signal can be used to directly recover the original message m(t).

Finally, the real FM equation can also be represented as a complex FM signal through the Euler identity. Recall Equation (2.5)

$$X_{FM}(t) = A_c \cos(w_c t + P(t)_{FM})$$

which can be written as

$$X_{FM}(t) = \operatorname{Re}\left[A_{c} \cdot e^{j \cdot P(t)_{FM}} e^{j \cdot w_{c}t}\right] = \operatorname{Re}\left\{A_{c} \cdot e^{j \left[w_{c}t + P(t)_{FM}\right]}\right\}$$
(2.9)

2.2 FM Demodulation Using Slope Detection

One type of conventional analog FM demodulation is achieved by determining the instantaneous frequency of an FM generated signal. In theory, an ideal frequency modulation (FM) detector is a device that produces an output that is proportional to the instantaneous frequency of the input. A common method of analog FM demodulation is called slope detection. Slope detection is a type of FM-to-AM conversion. Figure 2.1

shows a block diagram of a typical analog FM demodulator using slope detection [Cou90].



Figure 2.1 FM Demodulation for an Analog System Using Slope Detection

The slope detection method revolves around a differentiation operation that exploits the instantaneous frequency of the FM signal. The FM input signal is first subjected to a limiter in order to eliminate any amplitude modulation (AM) noise present in the signal. The output of the limiter is a square wave with constant amplitude. The square wave is then sent through the bandpass filter (BPF). The BPF has a center frequency of w_c and a bandwidth equal to the bandwidth of the FM signal. The BPF filters out the square wave harmonics and returns a constant-amplitude sinusoid. The constant-amplitude FM signal is then differentiated. The differentiation of the cosine carrier function exploits the instantaneous frequency of the FM signal by the property of the chain rule. Now, the instantaneous frequency can be thought of as the time-varying amplitude of the cosine carrier function. The instantaneous frequency is converted to an AM signal riding on top of the FM carrier function. This is where the principle of FM-to-AM conversion originates. The last step is to subject the differentiated FM signal to an envelope detector. The envelope detector extracts the amplitude, or envelope, of the input signal of interest. In the slope detection case, the extracted envelope is the instantaneous frequency of the FM signal, which contains the original message m(t). In conclusion, FM demodulation using slope detection recovers the original message m(t) by determining the instantaneous frequency of the FM signal.

2.3 Derivation of a Complex FM Signal at Baseband

An FM signal at baseband, or zero frequency, is the result of "mixing out" the carrier frequency from the FM signal, as shown in Figure 2.2. Thus, the carrier frequency no longer appears in the FM equation. In this paper, the availability of a complex-valued baseband FM signal is the major advantage in designing the digital FM demodulator. For this reason, the representation of a complex-valued FM signal at baseband is derived. Figure 2.2 depicts the generation of a complex baseband FM signal from a conventional FM signal.

The generation of complex data is the result of mixing the FM signal with a cosine and sine local oscillator (LO). This process can be derived mathematically by using the complex version of the FM equation. The mixing process is a simple multiplication of signals. The cosine mixing term and sine mixing term are multiplied with the incoming FM signal. For baseband results, both mixers oscillate at the FM carrier frequency w_c. The total mixing operation produces a real (in-phase) and imaginary (quadrature-phase) baseband component.



Figure 2.2 Generation of a Complex Baseband FM Signal

Adding the in-phase and quadrature-phase baseband components results in the complex baseband FM signal. The derivation of these components is accomplished with the aid of Figure 2.2. The symbol \otimes below denotes a mixing (multiplication) operation.

2.3.1 In-Phase Baseband Component

In-phase component =
$$\operatorname{Re}\left[A_{c} \cdot e^{j \left[w_{c}t + P(t)_{FM}\right]}\right] \otimes \cos(w_{c}t)$$
 (2.10)
Using the identities: $\operatorname{Re}[z] = \frac{z + z^{*}}{2}$, where z is a complex number
 $\cos(x) = \frac{e^{jx} + e^{-jx}}{2}$, Euler's identity

gives

$$= \frac{A_{c} \left\{ e^{j \left[w_{c}t + P(t)_{FM} \right]} + e^{-j \left[w_{c}t + P(t)_{FM} \right]} \right\}}{2} \cdot \frac{e^{j w_{c}t} + e^{-j w_{c}t}}{2}$$
(2.11)

$$= \frac{A_c}{4} \left\{ e^{j [2w_c t + P(t)_{FM}]} + e^{jP(t)_{FM}} + e^{-jP(t)_{FM}} + e^{-j [2w_c t + P(t)_{FM}]} \right\}$$
(2.12)

$$= \frac{A_c}{2} \cdot \left[\operatorname{Re} \left\{ e^{j \left[2 w_c t + P(t)_{FM} \right]} \right\} + \operatorname{Re} \left\{ e^{j P(t)_{FM}} \right\} \right]$$
(2.13)

For conventional FM signals, the carrier frequency w_c is much greater than message frequency m(t). The first complex exponential term in Equation (2.13) is the upconverted term since its carrier frequency has been translated to a frequency of $2w_c$. The second complex exponential term in Equation (2.13) is the down-converted term since its carrier frequency has been translated to zero frequency. Reviewing Figure 2.2 and using the fact that $w_c \gg w_{m(t)}$, the low-pass filter extracts the down-converted (baseband) term and filters out the up-converted term. Thus, the real baseband component of the FM signal can be represented by the following equation.

In-phase baseband component =
$$\frac{A_c}{2} \cdot \operatorname{Re}\left[e^{jP(t)_{FM}}\right]$$
 (2.14)

2.3.2 Quadrature-Phase Baseband Component

Quadrature-phase component = $\operatorname{Re}\left[A_{c} \cdot e^{j\left[w_{c}t + P(t)_{FM}\right]}\right] \otimes \sin(w_{c}t)$ (2.15) Using the identities: $\operatorname{Im}[z] = \frac{z - z^{*}}{2}$, where z is a complex number $\sin(x) = \frac{e^{jx} - e^{-jx}}{j2}$, Euler's identity

$$= \frac{A_{c}\left\{e^{j[w_{c}t+P(t)_{FM}]}-e^{-j[w_{c}t+P(t)_{FM}]}\right\}}{2} \cdot \frac{e^{jw_{c}t}-e^{-jw_{c}t}}{j2}$$
(2.16)

$$= \frac{A_{c}}{i4} \left\{ e^{j[2w_{c}t + P(t)_{FM}]} - e^{jP(t)_{FM}} + e^{-jP(t)_{FM}} - e^{-j[2w_{c}t + P(t)_{FM}]} \right\}$$
(2.17)

$$= \frac{A_c}{j2} \cdot \left[\operatorname{Im} \left\{ e^{j [2w_c t + P(t)_{FM}]} \right\} - \operatorname{Im} \left\{ e^{jP(t)_{FM}} \right\} \right]$$
(2.18)

Reviewing Figure 2.2, the low-pass filter extracts the down-converted (baseband) term in Equation (2.18) and filters out the up-converted term in Equation (2.18). Thus, the imaginary baseband component of the FM signal can be represented by the following equation.

Quadrature-phase baseband component =
$$j \frac{A_c}{2} \cdot \text{Im}\left[e^{jP(t)_{FM}}\right]$$
 (2.19)

Now, the complex baseband FM signal can be written as the sum of Equations (2.14) and (2.19), the in-phase and quadrature-phase baseband components.

$$X(t)_{FM_{baseband}} = \frac{A_c}{2} \cdot \left[\operatorname{Re}\left\{ e^{jP(t)_{FM}} \right\} + j\operatorname{Im}\left\{ e^{jP(t)_{FM}} \right\} \right]$$
(2.20)

or,

$$X(t)_{FM_{baseband}} = \frac{A_{c}}{2} \cdot \left\{ \cos[P(t)_{FM}] + j\sin[P(t)_{FM}] \right\} = \frac{A_{c}}{2} e^{jP(t)_{FM}}$$
(2.21)

The design of the digital FM demodulator hinges on Equation (2.21). This complex baseband FM equation will be referred to during the FM demodulator development phase. By inspection of Equation (2.21), the complex FM signal at baseband is represented as a complex exponential function with a varying frequency directly related to $P(t)_{FM}$. The complex baseband FM signal can also be demodulated using standard analog methods. A demonstration of complex baseband FM demodulation by the slope detection method is presented next.

2.4 Analog FM Demodulation of a Complex FM Signal at Baseband

With the aid of Figure 2.1, the demodulation of the complex baseband FM signal using the slope detection method is presented. Recall the complex baseband FM equation from Equation (2.21).

$$X(t)_{FM_{baseband}} = \frac{A_c}{2} e^{jP(t)_{FM}}$$

The input signal first passes through the limiter circuit. Assume that the limiter transforms the input signal to a square wave with amplitude V_c . At the output of the BPF, the FM signal is recovered and takes the form.

$$X(t)_{FM_{\text{imitebpf}}} = V_{c} e^{jP(t)_{FM}}$$
(2.22)

Following Figure 2.1, the signal next passes through the differentiation block. After differentiating, the FM signal can be represented by

$$X(t)_{FM_{\text{im-bpf-diff}}} = V_{c} \left(j \frac{\partial P(t)_{FM}}{\partial t} \right) \cdot e^{jP(t)_{FM}}$$
(2.23)

The last block in Figure 2.1 is the envelope detector. The envelope detector extracts the magnitude of the signal.

$$X(t)_{FM_{\text{im-bpf-diff-ed}}} = \left| V_{c} \left(j \frac{\partial P(t)_{FM}}{\partial t} \right) \cdot e^{jP(t)_{FM}} \right| = V_{c} \cdot \frac{\partial P(t)_{FM}}{\partial t}$$
(2.24)

Recall from Equation (2.4), the original message m(t) is the derivative of $P(t)_{FM}$. Thus, the demodulated result is

$$X(t)_{FM_{\text{temodulated}}} = V_{c} \cdot \left[D_{f} \cdot m(t) \right]$$
(2.25)

or,

$$X(t)_{FM_{\text{demodulated}}} = \mathbf{C} \cdot \mathbf{m}(t)$$
 (2.26)

where C is a constant value.

Equation (2.26) proves that demodulating a complex analog baseband FM signal using the slope detection method yields the original message m(t). This conclusion is used

to justify the algorithm development of the digital FM demodulator. Hence, the theoretical foundation for the digital FM demodulator development has been established using an analog approach.

CHAPTER 3 DIGITAL RADIO HARDWARE AND SYSTEM ARCHITECTURE

This chapter discusses the system architecture and major hardware components on the digital radio board. Recall, the FM demodulator algorithm design revolves around the availability of complex-valued baseband digital data from the digital radio hardware. This demonstrates a classic case of designing software around the capabilities of the available hardware.

3.1 The Single-Channel Digital Radio

3.1.1 Architectural Overview

The digital radio is a single-channel communications-based receiver. Different from its analog counterpart, the digital radio consists of all digital components and performs all signal processing without traditional analog circuitry. The digital radio is able to process narrowband signals extracted from a digitized wideband RF source [Gra91]. The architecture of the digital radio board provides a flexible radio-frequency (RF) receiver that is controlled strictly through software. The receiver has the advantage of processing RF signals in the digital domain, which allows digital signal processing (DSP) methods to be employed. This versatile architecture dwarfs the analog receiver in that one digital radio can be programmed to perform unlimited tasks which are custom to the user.

The digital radio architecture is a flexible microprocessor-based design centered around a Gray GC1011 digital receiver chip. The GC1011 chip is responsible for receiving the incoming RF digitized data, down converting it to baseband, lowering the sampling rate of the data, and piping it to a host processor for computation and processing. A generic block diagram of a digital radio architecture is shown in Figure 3.1 [Gra91].



Figure 3.1 Single-Channel Digital Radio Block Diagram

3.1.2 Major Hardware Components of the Digital Radio

The digital radio board is a surface-mount design (SMD) printed-circuit (PC) board and runs at a clock speed of 50 MHz. The SMD is needed to realize a high-speed digital board with clock speeds in this range. A general overview of the major components are described below. These components implement the major blocks shown in Figure 3.1.

High-speed analog-to-digital converter

The analog-to-digital (A/D) converter used in the digital radio is a high-speed Analog Devices 100 Msamples/second ECL flash A/D with 8-bit resolution. It is clocked at 50 MHz, feeding 50 Msamples/second of digital RF data to the GC1011 digital receiver chip. The flash A/D was necessary to obtain the conversion speeds needed for the GC1011. A small analog circuit is located before the A/D converter to precondition the incoming RF analog signal and to maintain a stable reference voltage for the A/D.

Gray GC1011 digital receiver chip

The Gray GC1011 digital receiver chip is the heart of the digital radio. It is responsible for processing the incoming wideband RF digital data and sending the resultant narrowband output data to the host processor for analysis. The GC1011 receives its digital RF data from the high-speed A/D converter. The GC1011 can receive 12-bit input data samples but is constrained to 8-bit input data due to the hardware limitations of a 12-bit flash A/D at the time of the board construction. The GC1011 is controlled by a host processor via the peripheral interface. The host processor configures the GC1011 by writing to control registers onboard the GC1011. There are sixteen 8-bit control registers that can be accessed through the GC1011's bi-directional data lines. The four address lines of the GC1011 are used to address the desired control register. Some major GC1011 functions that the host processor is able to control include the following: GC1011 tuning frequency, output data decimation rate, output data spectral formatting, signal gain, and output data format. A functional description of a typical GC1011 tasking is listed below.

- The digitized RF data are received by the GC1011 and mixed with the tuning frequency, which effectively down converts the RF signal to baseband.
- The baseband data are decimated via a programmable low-pass filter cascaded with a decimate-by-four low-pass filter in order to lower the output bandwidth of the signal.
- Finally, the data are formatted and sent to the host processor. The data formats include complex or real output data and flipping or offsetting the output spectrum.

Specifically, the major feature exploited from the Gray GC1011 digital receiver chip is the generation of complex baseband data . This is an important innovation used to design the digital FM demodulator.

One limitation of the GC1011 is the ability to tune up to a maximum frequency of half its operating clock rate. Thus, at a 50 MHz clock speed, the digital radio can directly digitize and tune to RF frequencies from 0 to 25 MHz. The GC1011 is a memory-mapped peripheral in the host processor's external memory map. The host processor configures the GC1011 and controls the GC1011 during program execution by communicating to the command registers [Gra91].

Host processor

The host processor for the digital radio is a one-instruction-per-cycle digital signal processor (DSP) chip. A fast DSP processor is needed to handle the flow rate of data sent from the GC1011. The DSP residing on the digital radio board is an Analog Devices ADSP-2101, 16-bit fixed-point processor running at a 16 MHz clock (instruction) rate. The ADSP-2101 is a Harvard architecture RISC microprocessor, i.e., separate program and data memories and respective memory maps. All peripherals, including the GC1011, are memory mapped into the ADSP-2101's external data memory map. The DSP directly retrieves parallel digital data from the GC1011 and is able to send the processed results to a digital-to-analog converter (DAC) for analog output. The DSP runs the operating system software and performs all housekeeping and computational tasks for the digital radio board. On powerup or system reset, the DSP automatically boots from an onboard EPROM that contains its tasking software [Ana90].

Digital-to-analog converter

The back-end digital-to-analog converter (DAC) is a Burr-Brown 12-bit dual converter. It is used to retrieve the processed digital data from the DSP and convert it to an analog output. The output sample rate for the DAC is set by the host processor. The host writes the desired sample time to a hardware timer that is connected to the DAC load lines. This architecture allows the DAC timer to interrupt the processor when it times out. This hardware methodology achieves a stable, constant sampling interval that is not software dependent. In this design, the demodulated FM data was sent from the host processor to the DAC for analog audio output.

3.2 Performance Capabilities of the Digital Radio

3.2.1 Capturing High-Frequency RF Signals with the Digital Radio

An inherent bottleneck of the digital radio surfaces when targeting very-high frequency (VHF) and ultra-high frequency (UHF) signals. In order to process VHF and UHF radio signals, a front-end analog down converter must be used in conjunction with the digital radio in order to down convert the band of interest into the GC1011's tuning range. Recall, the GC1011 can only directly tune up to a maximum frequency of 25 MHz with a 50 MHz clock rate. This specification limits the range of frequencies accessible to the digital radio board. Specifically, any frequency over 25 MHz cannot be received by the digital radio without the use of a front-end analog down converter. For this paper, this was not a problem since the FM modulated signal was generated with a carrier frequency within the GC1011 tuning range. However, in practical use this problem can be alleviated by using a standard VHF/UHF receiver as the down converter. The intermediate frequency (IF) output from the VHF/UHF receiver can be used as the GC1011's tune frequency. The two most common IF frequencies for FM systems are 10.7 MHz and 21.4 MHz. The GC1011 can directly tune up to either of these IF frequencies. The output IF frequency from the VHF/UHF receiver is just the down-converted term of the RF signal. Hence, this IF frequency can be used as the RF input to the digital radio, while the GC1011 tune frequency is set to the VHF/UHF receiver's IF frequency. Since the GC1011 is constantly tuned up to the IF, the digital radio can now process any frequency the front-end VHF/UHF receiver can supply.

3.2.2 Advantages and Disadvantages of a Digital Radio Architecture

The digital radio performs signal processing tasks via software. This software is run by the host DSP processor, which configures the hardware on the board and performs all computational tasks relevant to the desired signal processing task. Thus, by changing the DSP software, the digital radio effectively becomes a custom narrowband receiver. Multiple narrowband demodulators, modems, or communication-based algorithms can be easily implemented on the digital radio. This exemplifies the digital radio's signal processing flexibility over the conventional single-task analog receiver.

However, there are a few drawbacks to a digital radio architecture at this phase. First, it is unable to tune up to VHF or UHF signals without the help of an analog down converter. Secondly, only narrowband signals can be processed from a wideband RF input. The processing speed of the DSP and GC1011 limits the computational throughput of the radio. For these reasons, wideband signal processing is generally not feasible using the current design of the digital radio architecture.

3.3 Overview of the Gray GC1011 Digital Receiver Chip

Because of the importance of the GC1011 digital receiver chip in the digital FM demodulator design, a block diagram illustrating the major functions of the GC1011 is presented. A block diagram of the GC1011 is shown in Figure 3.2.



Figure 3.2 Block Diagram of the GC1011 Internals

A brief description of each of the major blocks in Figure 3.2 is presented to introduce the novel hardware functionality of the GC1011.

3.3.1 Control Interface

The control interface allows an external host processor to communicate with the GC1011's internal registers. The host processor is able to configure the GC1011 by writing to the registers in the control interface. The control interface consists of sixteen 8-bit registers, which are addressed using the GC1011 data bus and address lines. The

GC1011 has eight bi-directional data lines (D7-D0) and four address lines (A3-A0). An active low chip select (/CS) and read/write pin (R/W) are used to access the chip using standard memory-mapped peripheral protocols. Also, the resulting 16-bit real (I) and imaginary (Q) data from the GC1011 is read by the host processor by accessing the proper data control registers [Gra91]. Because the GC1011 is limited to an 8-bit data bus, this requires four parallel register reads in order to assemble the 16-bit I and Q output samples.

3.3.2 Digital Oscillator and Mixer

The digital oscillator is responsible for generating the sine and cosine discrete sequences which are mixed with the incoming digital data X11-X0. The digital oscillator consists of a 28-bit frequency register, accumulator, and sine-cosine digital word generator. The tuning frequency of the digital oscillator is set by loading the frequency register with the calculated tuning frequency using the below equation [Gra91].

$$FREQ = \frac{2^{28} (\text{Desired tuning frag})}{\text{Clock rate}}$$
(3.1)

where FREQ is the 28-bit frequency register. The FREQ register is loaded by writing a frequency word from the host processor to the frequency register in the digital oscillator.

The upper 13 bits of the 28-bit FREQ word are used to generate the digital oscillator's sine and cosine digital sequences. The resulting digital samples are rounded to 12 bits. Using the 6-dB rule [Cou90], this allows a maximum of 6(12) = 72 dB of spurious free dynamic range for the oscillator.

The digital mixer simply multiplies the incoming 12-bit samples (X11-X0) with the 12-bit sine and cosine sequences. The output of the mixer is a digital sequence at zero frequency. Thus, mixing an input signal with its carrier frequency equal to the digital

oscillator's tuning frequency results in a baseband digital sequence. In other words, the input sequence is centered at zero frequency after passing through the mixer.

3.3.3 Programmable Low-Pass Filter

The output of the mixer is fed into a programmable low-pass filter in order to isolate the down converted baseband sequence. The filter also decimates the sequence. In other words, the filter lowers the sample rate of the sequence by a factor of D [Gra91]. The value of D can range from 16 to 16,384. This parameter is configured by writing to the BANDWIDTH control register [Gra91], which is illustrated in Figure 3.2.

3.3.4 Decimate-by-Four Low-Pass Filter

The decimate-by-four filter is a fixed low-pass finite-impulse-response (FIR) decimation filter that further decimates the baseband sequence by four after the initial programmable low-pass filter. The total sample rate reduction is therefore 4D.

Because of the initially high incoming sample rate, the reduction is necessary in order to process the embedded modulated signal in real time. Because of the possibility of aliasing, the reduced sample rate must still meet Nyquist's criteria. In other words, the output sequence from the final decimation filter must still maintain a sample rate at least two times the maximum frequency in the modulated signal. Obviously, this decimation parameter depends on the bandwidth of the desired demodulated signal. Control registers GAIN and FILTER SELECT exist to correct the filter gain and select one of two FIR decimation filter types. The decimation filter can either have a 3 dB passband with 70 dB attenuation in the stop band covering 80% of the Nyquist rate, or a 3 dB passband with 50 dB attenuation in the stop band covering 90% of the Nyquist rate [Gra91].

3.3.5 Output Format

The output format block receives the resulting samples from the lowpass filter network. The output samples are rounded to 16 bits, and the output spectrum is optionally flipped, converted from a complex to a real spectrum, or offset by one-fourth the Nyquist rate [Gra91]. The control word written to the filter control register governs the formatting of the output samples. The resulting 16-bit I and Q samples are sent to the output storage registers for the host to access. Due to the 8-bit data bus, the host must perform four parallel reads to retrieve one complex sample from the GC1011. Moreover, the digital radio board has no GC1011 interrupt capability, so the host must "poll" the GC1011 in software to determine when a new sample is ready. The ramifications of software polling is a decrease in the DSP real-time processing window. A software polling loop requires more DSP instructions than an interrupt-service subroutine, causing the decrease in the real-time processing window. Other important implementation issues and inherent hardware limitations are discussed in later chapters.

CHAPTER 4 ALGORITHM DEVELOPMENT OF THE DIGITAL FM DEMODULATOR

This chapter discusses the development of the digital FM demodulator using the theoretical and hardware foundations discussed in the previous chapters. In order to demodulate a digitally-sampled FM signal, a digital method of determining the instantaneous frequency of the sampled FM signal is needed. Chapter 2 presented the analog approach of demodulating a complex-valued FM signal at baseband. These mathematical steps will be transformed into their digital equivalents, creating a digital FM demodulator. The end result of this chapter is to fabricate a fast digital FM demodulator able to run on the digital radio's DSP. Therefore, the attributes of the digital radio board also governs the design strategy for the demodulator.

4.1 Complex Vector Representation

Figure 4.1 displays the complex Cartesian coordinate system and the complex unit circle |z| = 1. From Equation (2.21), the complex equation for an FM signal at baseband, a complex-valued FM sample can be represented by a vector on the complex unit circle having an amplitude and a phase angle. A complex sample gives two pieces of information, a real and imaginary component. The polar form of a complex number z, where z = x + j y, can be represented by the following equations.

$$z = r \cdot e^{j\theta} \tag{4.1}$$

$$r = \sqrt{x^2 + y^2} \tag{4.2}$$

$$\theta = \tan^{-1} \frac{y}{x} \tag{4.3}$$

Figure 4.1 labels the quadrants in the complex coordinate system the same as the standard Cartesian rectangular system.



Figure 4.1 Complex Coordinate System

The polar form of a complex number, shown in Equation (4.1), can be used to extract the phase angle of a complex sample. Each incoming complex sample will have a new amplitude and phase angle. Since FM signals store all of their information in the phase, this chapter proves that the phase angle is the information required to demodulate a complex-sampled FM signal.

Successive complex-valued samples can be shown to "rotate" around the complex unit circle in Figure 4.1. For example, if a sinusoid with a constant frequency is complex sampled, each consecutive sample can be represented as a vector rotating around the complex unit circle. The degrees of advancement between consecutive samples can be expressed by the following equation.

$$\Delta \theta = \frac{\text{frequency of signal}}{\text{sample rate}} \cdot 360^{\circ} \tag{4.4}$$

Equation (4.4) is used to directly relate the phase difference between two complexvalued samples. In the previous example, suppose the sinusoid is sampled at a rate eight times greater than its frequency. Applying Equation (4.4), each vector will travel $(1/8)(360^\circ) = 45^\circ$ from the previous sample's location. Furthermore, at the Nyquist sampling rate, or $2f_{max}$, each successive vector will travel 180° from the last vector's position. The previous finding demonstrates the key result of the sampling theorem [Str88]. In order for aliasing not to occur in the sampled signal, consecutive vectors cannot advance more than 180°.

4.2 Mathematical Modeling of the Digital FM Demodulator

4.2.1 The Polar Discriminator

As stated in the above section, the phase angle contains the necessary information needed to demodulate a complex-sampled FM signal. Chapter 2 presented the mathematical foundation supporting this method of FM demodulation for complex FM signals at baseband. Specifically, determining the instantaneous frequency of the FM signal recovers the original message.

One approach for determining the digital instantaneous frequency of a complexsampled FM signal is by using a polar discriminator. A polar discriminator measures the phase difference between consecutive samples of a complex-sampled FM signal. This phase difference turns out to be the instantaneous frequency of the sampled FM signal. A polar discriminator operates by taking successive complex-valued samples and multiplying the new sample by the conjugate of the old sample. Consider two consecutive complex-valued baseband FM samples with unity magnitude and phase angles Θ_1 and Θ_2 , respectively. The polar discriminator can be represented mathematically in polar form by using Equation (2.21).

$$FM_{\text{baseband}} = e^{j\theta_1} \tag{4.5}$$

$$FM_{baseband} = e^{j\theta_2} \tag{4.6}$$

$$\mathbf{e}^{j \cdot (\theta_2)} \cdot \mathbf{e}^{-j \cdot (\theta_1)} = \mathbf{e}^{j \cdot (\theta_2 - \theta_1)}$$
(4.7)

Equation (4.7) is the result of the polar discriminator. The polar discriminator takes two complex-valued samples with different phase angles and returns the phase difference between the samples. Note that the difference operation in the digital domain is an approximation of a time differentiation in the analog domain. For discrete-time systems this differentiation can be represented as a backward-difference equation similar to the equation below [Str88].

$$\frac{\partial f(t)}{\partial t} \approx \frac{1}{T} \left[f(nT) - f((n-1)T) \right]$$
(4.8)

In Equation (4.8), f(t) is a continuous function, T is the sampling period, and n is a positive integer. Equation (4.8) reveals that the difference operation in Equation (4.7) approximates the derivative of the FM phase. Actually, using the concepts of finite-difference calculus shows that Equation (4.8) is exact for first-order functions.¹ Therefore, the polar discriminator in Equation (4.7) calculates the exact phase derivative for signals with first-order frequency characteristics. A polar discriminator returns the

¹ From William Hager, "Numerical Analysis Lecture Notes", University of Florida, 1992.

exact phase derivative for sinusoids with a constant frequency. Moreover, a sinusoid with a varying frequency (i.e., an FM signal with a sinusoidal message) causes the polar discriminator to return an approximation of the phase derivative. This differentiation error is due to the fact that Equation (4.7) is no longer exact for phase functions greater than first order. However, if the sampling period T is made sufficiently small, it can be shown that a nonlinear function exhibits a linear behavior between closely-spaced sample points [Str88]. Thus, a small sampling period T increases the accuracy of the polar discriminator for a sinusoidal input with a nonlinear frequency.

Equations (2.4) and (4.7) show that the calculated derivative from the polar discriminator is equivalent to the instantaneous phase of the sampled FM signal. This instantaneous phase is synonymous with the instantaneous frequency of an analog FM signal. Therefore, the phase difference between the two consecutive complex-valued FM samples is the information needed to demodulate the sampled FM signal. A signal flow graph of a polar discriminator is displayed in Figure 4.2.



Figure 4.2 Signal Flow Graph of a Polar Discriminator

The polar discriminator operates on a sample-by-sample basis. When a new complex sample arrives in the discrete-time system, a new phase-difference vector is

calculated. Some of the key characteristics of the polar discriminator when operating on a sampled FM input signal are listed below.

- A sampled sinusoid with a constant frequency (no modulation) results in vectors residing at the same location on the unit circle. Recall the case of the sampled sinusoid with a 45° advancement between samples. By Equation (4.7), the output of the polar discriminator is a vector with a phase angle equal to 45°. Therefore, subjecting an unmodulated sinusoid to a polar discriminator produces vectors with a constant phase angle. This constant phase angle can be computed using Equation (4.4).
- The origin is equivalent to a vector with a phase angle equal to zero. By definition, a baseband FM signal is centered at zero frequency. Thus, subjecting a complex-sampled baseband FM signal to a polar discriminator results in vectors that migrate about the origin. Figure 4.3 displays the origin as the line Im(z) = 0, Re(z) > 0.
- For a baseband FM signal, the polar discriminator vectors migrate about the origin according to the frequency deviation of the FM signal. At any point in time, if the FM signal has a frequency greater than the carrier frequency w_c , then the polar discriminator vector resides in quadrant I or II and has a positive phase angle. Likewise, if the FM signal has a frequency less than the carrier frequency w_c , then the polar discriminator vector resides in quadrant I or III and has a positive phase angle. Likewise, if the FM signal has a frequency less than the carrier frequency w_c , then the polar discriminator vector resides in quadrant IV or III and has a negative phase angle. Figure 4.3 demonstrates this concept for two vectors residing in quadrants I and IV, respectively.
- The maximum attainable phase angle of a polar discriminator vector depends on the sampling rate. By the sampling theorem, if an FM signal is sampled at the Nyquist rate or higher, then the polar discriminator vectors are constrained to have phase angles less than 180°.
- If a baseband FM signal is oversampled at a rate of four times or greater, then the polar discriminator vectors are constrained to rotate within quadrants I and IV. The sampling rate governs the number of degrees the polar discriminator vectors migrate from the origin. Therefore, using Equation (4.4), a four times oversampling rate results in vectors deviating a maximum of 90° from the origin. Thus, increasing the sampling rate decreases the distance (in degrees) the polar discriminator vectors deviate from the origin.


Figure 4.3 Vector Diagram of the Polar Discriminator Results

In summary, utilizing a polar discriminator on successive complex-valued baseband FM samples gives the instantaneous frequency of the sampled FM signal. The resulting phase angle from the polar discriminator result contains the information in the original message m(t).

4.2.2 Digital Limiter and Phase Angle Approximation

The difficult step of recovering the message information from a sampled FM signal is determining the phase angle from the polar discriminator result. The polar discriminator returns a complex number z = x + j y. The corresponding phase angle of that complex number is the instantaneous frequency of the sampled FM signal. From Equation (2.26), this result is exactly the message m(t). Equation (4.3) shows the exact method of determining the phase angle θ of a complex number. The true phase angle calculation involves the arctangent function. Consequently, the arctangent is not an intrinsic function in any DSP or microprocessor instruction set. Furthermore, computing a true arctangent is complex and too time consuming for most DSP applications. Thus, an estimate of the arctangent which gives an accurate measure of θ is necessary. There are many methods for approximating the phase angle of a complex number, and one such method which is geared for speed is developed in this chapter.

Consider again the complex coordinate system in Figure 4.1. Using Equation (4.3), the phase angles in quadrants I and II are all positive (0 to π radians). The phase angles in quadrants III and IV can be considered as negative angles ($-\pi$ to -2π radians). In fact, the angles in quadrants III and IV are the exact negatives of the angles in quadrants II and IV are the exact negatives of the angles in quadrants II and I, respectively. Therefore, an approximation of the phase angle θ only needs to be derived for quadrants I and II. This approximation can be translated to quadrants III and IV by a simple negation.

Development of a digital limiter

In FM the amplitude of the signal is assumed to be constant. However, amplitude modulation (AM) noise and other contributing factors can vary the amplitude of the resultant vector from the polar discriminator. A varying amplitude will cause errors in the phase approximator. The phase approximation must be invariant to the amplitude of the polar discriminator vector. Recall from Chapter 2 that analog FM demodulators, like the slope detector in Figure 2.1, solve this problem by using a hard limiter to clip the signal amplitude to a known value.

In the digital mathematical model, it was discovered that a ratio of the real component and imaginary component always gives a result that is phase dependent and amplitude independent. These ratios correspond to a range of numbers that are native to each quadrant. Consider quadrant I shown in Figure 4.1. The real and imaginary components of a complex number are positive in quadrant I. A ratio that is amplitude independent is

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$$ratiq_{uadranI} = \frac{\text{Re}(z) - \text{Im}(z)}{\text{Re}(z) + \text{Im}(z)}$$
(4.9)

Equation (4.9) relates the real and imaginary components to their position in quadrant I, but the result does not depend on their amplitude. This result still preserves the phase, but the division operation makes it amplitude invariant. The ratio in Equation (4.9) returns real numbers in the range [-1,1]. The equation below shows the critical points returned by the quadrant I ratio.

$$ratiq = \begin{cases} 1, & \text{Re}(z) \neq 0, \text{ Im}(z) = 0\\ 0, & \text{Re}(z) = \text{ Im}(z)\\ -1, & \text{Re}(z) = 0, \text{ Im}(z) \neq 0 \end{cases}$$
(4.10)

Equation (4.10) reveals that the ratio in Equation (4.9) returns fractional results. Thus any vector, invariant of its magnitude, residing in quadrant I will return a unique number that is relative to its phase in quadrant I. This unique number will be a fractional number in the range [-1,1]. The fractional result is another design characteristic of the ratio. The demodulator software will run in a fixed-point (fractional) mode on the DSP. Thus, the ratio already addresses the problem of obtaining fractional numbers for the calculations on the DSP. Using the same methodology, the ratio for complex numbers residing in quadrant II is

$$ratiq_{uadranII} = \frac{\text{Re}(z) + \text{Im}(z)}{\text{Im}(z) - \text{Re}(z)}$$
(4.11)

Equation (4.11) also returns fractional numbers within the range [-1,1]. Recall from Figure 4.1, imaginary components are positive and real components are negative in quadrant II. Similar to Equation (4.10), the ratio for quadrant II returns the following critical points.

$$ratiq_{I} = \begin{cases} 1, & \text{Re}(z) = 0, \text{ Im}(z) \neq 0 \\ 0, & \text{Re}(z) = \text{ Im}(z) \\ -1, & \text{Re}(z) \neq 0, \text{ Im}(z) = 0 \end{cases}$$
(4.12)

Finally, Equations (4.9) and (4.11) can be computed for all values of a complex number z in each respective quadrant. As shown, these ratios not only give a means to estimate the phase, but they also perform the same task as a hard limiter. Therefore, the digital FM demodulator is not subject to AM noise.

Development of a phase angle estimate function

In order to estimate the actual phase angle returned by the ratios in Equations (4.9) and (4.11), a relationship between these calculated ratios and the true phase angle θ is needed. Recall, Equations (4.9) and (4.11) return fractional numbers in the range [-1,1]. These resulting numbers have to be converted to the actual phase angles of each complex number. Since the processing time for the DSP is finite, an approximation of the actual phase angle is sufficient. There exists many methods for approximating functions. Several popular methods include: Table look up, Taylor-series approximation, and polynomial fitting.

Polynomial fitting, or Lagrange interpolation, was chosen as the phase function approximation technique. This technique allows any continuous function to be "fitted" with a polynomial derived from actual data points.² The method can be used to create low-order polynomials that only need a few multiplies and additions to produce a sufficiently accurate function estimate. The ratios from Equation (4.9) and (4.11) act as the inputs to the Lagrange interpolating polynomial. The resultant polynomial is the phase angle estimate function. In this mathematical model, one interpolating polynomial is

² From William Hager, "Numerical Analysis Lecture Notes", University of Florida, 1992.

needed for the quadrant I ratio and another is needed for the quadrant II ratio. The construction of the quadrant I interpolating polynomial is shown in Figure 4.4. The difference table approach demonstrated in Figure 4.4 is indicative of Newton's method, but the resulting polynomial is equivalent to a Lagrange interpolation polynomial.³



Figure 4.4 Construction of the Quadrant I Interpolating Polynomial

For each interpolating polynomial, the three critical ratio points shown in Equations (4.10) and (4.12) were chosen to construct a second-order (quadratic) polynomial. For the case of quadrant I, the corresponding phase angle points that matched the critical ratio values were (in radians): $\theta = 0$, $\pi/4$, and $\pi/2$ (the two endpoints and the midpoint in the quadrant). For quadrant II, the corresponding phase angle points were: $\theta = \pi/2$, $3\pi/4$, and π . Finally, the interpolating phase estimate polynomials were

³ From William Hager, "Numerical Analysis Lecture Notes", University of Florida, 1992.

constructed following the method in Figure 4.4. The resulting phase estimate functions are

$$\theta_{quadrant} = -\frac{\pi}{4} \cdot ratiq + \frac{\pi}{4}$$
(4.13)

$$\theta_{quadranII} = -\frac{\pi}{4} \cdot ratiq_{I} + \frac{3\pi}{4}$$
(4.14)

Equations (4.13) and (4.14) show that the second-order polynomials simplified to first-order (linear) equations. These interpolating polynomials produce sufficient phase angle results. However, the first-order approximation induces large errors away from the data points used to produce the polynomial. Intuitively, this error originates because the phase estimate function is linear, but the true phase function of a complex number is nonlinear. Consequently, increasing the number of data points in the polynomial construction increases the polynomial order, but the increase in order modifies the function "fit". A larger-order polynomial may reduce the error, but the increase in computational complexity becomes an issue.

Figure 4.5 shows a graph of the true phase angles versus Equations (4.13) and (4.14) for $\theta = 0$ to π . The dashed line in Figure 4.5 indicates the true phase angle points, and the solid curve is a plot of the phase angle estimate functions for quadrants I and II. From Figure 4.5, it is evident that the phase angle estimate functions have zero error only at the true phase angle points that were used to construct the interpolating phase functions. This property is an artifact of Lagrange polynomial interpolation. Also, the error in the phase estimate increases at phase angles that are far away from the data points used to construct the interpolating phase error is zero at $\theta = 0$, $\pi/4$, $\pi/2$, $3\pi/4$, and π . These data points were the exact phase angle points used to construct the polynomials as demonstrated in Figure 4.4.



Figure 4.5 Graph of the True Phase Angles Versus the Phase Angle Estimates

Figure 4.5 explicitly shows the larger regions of phase angle error as the phase estimates deviate from the true phase angle values. However, for a linear phase estimation function, the "fit" is extremely good.

The goal in this chapter was to develop a very fast phase approximator that sufficiently estimates the phase angle for a sampled FM signal. Moreover, the phase estimator has to accommodate for maximum phase angle differences of 180° (the Nyquist sampling rate) between consecutive incoming samples. Hence, the linear approximation function of the phase angle θ proves to be computationally fast as well as sufficiently accurate.

4.3 Demodulator Algorithm Block Diagram



A final block diagram of the designed digital FM demodulator is shown below.

Figure 4.6 Block Diagram of the Digital FM Demodulator Algorithm

By inspection, the functional blocks in Figure 4.6 perform the same operations as the blocks in Figure 2.1, but not in the same order. From Figure 4.6, the digital FM demodulator calculates the instantaneous frequency first and then performs a limiting operation. The analog slope-detection method shown in Figure 2.1 reverses these two tasks.

Relevant issues involving the sampling rate and speed of the digital FM demodulator, the system error due to the phase angle estimates, and other implementation factors are considered in the next chapter.

CHAPTER 5 REALIZATION AND TESTING OF THE DIGITAL FM DEMODULATOR

This chapter discusses the realization of the digital FM demodulator and addresses the implementation issues arising from the demodulator algorithm and the digital radio architecture. Also, the simulation, realization, testing, and performance of the digital FM demodulator is presented and analyzed.

5.1 Implementation Issues

5.1.1 FM Signal Bandwidth

The FM input signal received by the digital radio must be processed in real time for successful demodulation to occur. Therefore, the digital demodulator software must be finished processing the current sample before the next sample is captured. Adhering to Nyquist's Theorem, the FM signal must be sampled at least twice the total bandwidth of the baseband FM signal [Opp89]. The FM baseband bandwidth can be found by using Carson's rule [Cou90].

$$B_{FM} = 2(\frac{\Delta F}{B} + 1)B = 2(\Delta F + B)$$
 (5.1)

In Equation (5.1), B is the bandwidth of the message m(t) and ΔF is the frequency deviation as defined in Equation (2.7). For a sinusoidal message, the bandwidth B is just the frequency of the sinusoid f_m.

The corresponding Nyquist sampling rate for the FM signal bandwidth is

$$f_s = 2B_{FM} = 4(\Delta F + B) \tag{5.2}$$

A bottleneck occurs when the sampling rate exceeds the time it takes the DSP software to process a sample. If the FM signal is significantly oversampled, the demodulator must still operate in a real-time processing window. Wideband FM signals generally cannot be targeted with the demodulator because of their large bandwidth and the finite processing speed of the DSP. This bottleneck is an artifact of the DSP instruction rate and the speed of the digital radio hardware. However, narrowband FM signals are attractive since they offer less computational burden. A narrow FM bandwidth is indicative of a small frequency deviation. In this case, the narrowband FM signal can be significantly oversampled without running the risk of falling out of the real-time computational window. Therefore, the digital FM demodulator was only tested on narrowband FM signals.

5.1.2 Complex Sampling

Any real-valued input sequence has a frequency spectrum that exhibits Hermitian symmetry about the origin. The negative frequency spectrum is simply the Hermitian mirror image of the positive frequency spectrum, denoted by $H(w) = H^*(-w)$ [Mit93]. In the design of Hilbert transformers, the negative frequency spectrum is discarded since it is not needed. An ideal Hilbert transformer corresponds to an all-pass filter with a $\pi/2$ phase shift for all frequencies [Mit93]. Passing a real-valued signal x(t) through a Hilbert transformer component denoted by

$$y(t) = x(t) * h(t) = x(t) + j \left[x(t) * \frac{1}{\pi t} \right]$$
 (5.3)

The frequency response of the ideal Hilbert transformer resembles the following equation.

$$H(w) = \begin{cases} 2, & w > 0 \\ 0, & w < 0 \end{cases}$$
(5.4)

The gain factor of two in Equation (5.4) is purely for mathematical convenience. Thus, by observing the spectrum created from Equation (5.4), the property of causality has been imposed in the frequency domain. By the Fourier transform property of duality, this suggests a complex-valued time domain signal. For this reason, complex-valued time signals whose Fourier transforms vanish for negative frequencies are often termed "analytic" signals [Mit93].

The sampling theorem proves that the Fourier transform of a sampled real-valued input signal x(t) results in periodic replicas of X(w). These replicas of X(w) are spaced apart by integer multiples of the sampling frequency to produce the periodic Fourier transform [Opp89].

For the case of a complex-valued time sequence, it was proven above that the frequency spectrum is halved because of the discarded negative frequency portion. Thus, the periodic frequency replicas created from complex sampling contain no information in the respective negative frequency regions. Figure 5.1 demonstrates frequency spectrum replication of X(w) due to complex sampling.



Figure 5.1 Spectrum of a Complex Signal Sampled at the Nyquist Rate

Figure 5.1 shows the frequency spectrum X(w) of a band-limited "analytic" signal x(t). The second spectrum $X_{s}(w)$ corresponds to the Fourier transform of the sampled complex-valued time sequence, termed an "analytic" sequence.

The sampling theorem also states that the Nyquist sampling rate must be obeyed if no aliasing occurs in the frequency domain. For real-valued signals, the Nyquist frequency occurs at $w = \pi/T_s$. This corresponds to a Nyquist rate of $f_s = 2f_{max}$. However, for an "analytic" sequence it is readily apparent from Figure 5.1 that the Nyquist rate can be reduced by a factor of two. This reduction stems from the fact that the spectrum contains only positive frequency information. This "half-band" spectrum allows the Nyquist frequency to be relaxed to a value of $w = 2\pi/T_s$. The corresponding Nyquist sampling rate is reduced to $f_s = f_{max}$ without aliasing in the frequency domain. Hence, the net effect of complex sampling a real-valued input signal results is an overall relaxation of the Nyquist sampling rate by two. Using the above arguments, the digital FM demodulator can use a sampling rate equal to $B_{FM}/2$ given in Equation (5.1). Aliasing will not occur if the FM signal is complex sampled at a rate of $B_{FM}/2$ samples/sec. Thus, the new FM bandwidth equation becomes

$$B_{FM_{complex}} = \frac{B_{FM}}{2} = 2(\Delta F + B)$$
(5.5)

and the relaxed Nyquist sampling rate becomes

$$f_{s_{relaxed}} = B_{FM_{complex}} = 2(\Delta F + B)$$
(5.6)

The reduction in the sampling rate due to complex sampling shown in Equation (5.6) increases the FM signal bandwidth the demodulator can process while maintaining a real-time processing window.

5.2 Computer Simulations of the FM Demodulator Algorithm

The digital FM demodulator was first tested using computer simulation. These simulations provided a mapping from the algorithm theory into a working model. The simulations also promoted a figure of merit for the FM demodulator algorithm. Assuming no quantization error or finite math errors, the computer simulations provided a sterile environment in order to classify the performance of the algorithm by itself. Moreover, the final FM demodulator simulation acted as a template to translate the demodulator model directly into DSP assembly code. Mathcad 4.0 was utilized to simulate the demodulator algorithm. The simulations were first broken up into two sessions: 1) The polar discriminator simulation and 2) The phase angle estimate function simulation. Once these

two simulations were verified to work as designed, they were assembled as part of the final digital FM demodulator simulation. Each simulation session can be found in the Appendix.

5.2.1 Polar Discriminator Simulation

The polar discriminator was simulated with a synthetic complex-valued input signal. The input signal contained no modulation so the polar discriminator vectors had a constant phase angle and could be correctly distinguished. A polar plot demonstrated that the polar discriminator indeed operated properly and returned the correct phase difference between two complex samples. The relevant graphs can be found in Appendix A.

However, as noted in Chapter 4, for a sinusoidal or nonlinear message m(t), the polar discriminator does not return the exact phase derivative, but an approximation. The differentiation error in the polar discriminator result is difficult to quantify, but will be addressed in the testing phase of the demodulator since the message m(t) is generally a sum of sinusoids or nonlinear function.

5.2.2 Phase Angle Estimate Simulation

The next simulation tested the phase angle estimate functions for all four quadrants. A synthetic complex-valued signal was generated for 5000 phase angle points spanning across quadrants I and II. The two interpolating phase angle estimate functions were calculated for the angles native to their quadrant. The resulting phase angle estimates were plotted against the true phase angles. The relative error accrued from the phase angle estimates was treated as a random variable. Since the location of a given phase angle is random in a modulated signal, the error of the estimated phase is also random. In this case, the expected value of the relative error gives a measure of the average error in an ensemble of complex data points. The average relative error for the phase due to the phase estimator alone was shown to be 7.2%. This mean error figure is relatively low and sufficiently accurate for the demodulator algorithm. During the demodulator testing phase, this mean error figure can be expected to increase due to finite word lengths, the sampling rate, and the statistics of the input signal. Recall that the phase angle estimate functions have zero error only at the true phase angle points that were used to construct the interpolating phase functions. If a high sampling rate or the statistics of the input signal constrains the polar discriminator vectors to rotate within a small area of a given quadrant, then the relative phase error can be large if the resulting phase estimate is far away from the true data points used to create the interpolating phase function. Moreover, the true phase angle points used in the construction of the interpolating polynomials were equally distributed across their native quadrants. The data points were distributed this way since the phase estimate function has to correctly classify all phase angles as equally as possible. Because every phase angle is equally probable, the interpolating function must account for an equally distributed error across each quadrant. The equally distributed data points used in the Lagrange interpolation method accounts for some minimization of this error. The polar plot in Figure 5.2 is a replica of the phase error plot in Appendix B. Figure 5.2 accentuates the areas in each quadrant where the phase estimate error is large.

The probability of consecutive vectors residing in a large error region of the phase estimate function unilaterally depends on the statistics of the FM input signal and is therefore analytically unsolvable. However, as long as the Nyquist rate is maintained, the relative phase error will be approximately 7.2% on average. Also, sampling the input signal greater than the Nyquist rate increases the probability that a given vector will lie in a large error region of the phase estimate function. This is an artifact of the Lagrange polynomial construction. If the sampling rate constrains the vectors to migrate about an area that induces a large error in the phase estimate, the overall phase estimate error will increase.



Figure 5.2 Polar Plot of the Phase Angle Estimates Versus True Phase Angles

5.2.3 FM Demodulator Algorithm Simulation

The FM demodulator algorithm simulation was analyzed at the Nyquist sampling rate -- the maximum sampling rate for which the demodulator can operate. The modulated input message m(t) injected into the FM demodulator was chosen as a 1 kHz sinusoid. The sinusoidal message permits an easy first-order analysis of the demodulator performance. The complex mixing operation and complex sampling operation was simulated by creating a complex baseband FM signal through the use of Equation (2.21). The P(t) signal was generated in the simulation for simplicity. Also, an oscillatory AM noise signal was generated and added to the baseband FM signal to demonstrate the function of the digital limiter. Upon demodulation, the message m(t) appeared as the derivative of P(t), as given by Equation (2.4). The resulting amplitude of the message m(t) was calculated and verified in the simulation.

Polar discriminator and digital limiter

The FM demodulator simulation established that the polar discriminator calculated the phase difference between successive complex FM samples. These phase vectors deviate up to 180°, verifying the Nyquist sampling rate. Also, the digital limiter effectively eliminated the AM noise present in the phase vectors and passed the results to the phase estimate functions. The relevant graphs are shown in Appendix C.

Phase estimate errors

The resulting mean phase estimate error was approximately 4%. This error figure is lower than the calculated phase error shown in the phase angle estimate simulation. However, the statistics of the input FM signal can cause the phase vectors to reside around a low error region in the interpolating phase polynomial, thus explaining the low phase error.

Spectral analysis

Discrete phase errors are difficult to measure while the FM demodulator is being tested. Hence, a spectral purity test was simulated to measure a theoretical versus practical signal-to-noise ratio (SNR) for the demodulated message. The spectral simulation demonstrated that at the Nyquist rate, the algorithm suffered a minimum 5 dB loss in the SNR ratio due to the demodulator algorithm. Figure 5.3 is a replica of the spectral simulation plot found in Appendix C. From Figure 5.3, it is evident that harmonics of the message frequency were responsible for the SNR loss. In fact, only the odd harmonics were accountable for the noise. These corrupting harmonics give the FM demodulator algorithm a minimum SNR error expected after implementation. The harmonic distortion due to the demodulator algorithm can be attributed to the differentiation error from the polar discriminator and the phase estimate error. Because of the complexity of analyzing the system error, the simulation is unable to delineate which error contributes the most to the harmonic distortion.



Figure 5.3 Spectral Analysis Plot of the Demodulated Message

The final FM simulation gave sufficient results and demonstrated that the mathematical model of the FM demodulator worked as designed. The system error in the demodulated message demonstrates the classic tradeoff of algorithm speed versus accuracy. Since this FM demodulator algorithm was geared for speed, some error must be

tolerated. The next step was to translate the final FM demodulator simulation into DSP assembly code in order to run on the digital radio board.

5.3 Realization of the FM Demodulator into DSP Code

From the FM demodulator block diagram in Figure 4.5, the number of necessary mathematical operations to process one complex FM sample can be readily determined. The polar discriminator block requires one complex multiply, which translates to four real multiplies and two additions. Likewise, the digital limiter needs two additions and one division. Finally, the phase estimator block requires one real multiply and one addition. So, demodulating a complex-sampled FM signal requires the following operations per sample: Five real multiplies, five real additions, and one division.

5.3.1 DSP Computational Overhead

The FM demodulator was directly implemented into ADSP-2101 assembly code using the final Mathcad simulation as a template. The software listing is included in the Appendix. The polar discriminator was implemented in 19 DSP assembly instructions (62.5 ns per instruction cycle). The digital limiter was implemented in 25 DSP instructions. The phase angle estimator was implemented with 10 instructions for the quadrant I estimate and 14 instructions for the quadrant II estimate. Thus, the computational overhead was approximately 54-58 DSP instructions per complex sample for the FM demodulator. This overhead does not include the time to fetch a new complex sample from the GC1011. Chapter 3 stated that the GC1011 chip was "polled" for new samples. The GC1011 software overhead is about 30 DSP instructions, which corresponds to (30)*62.5 ns = 1.875 µs of extra overhead for processing each sample. Also, the DAC interrupt service routine requires 10 DSP instructions, or 625 ns. Hence, the worst-case time it takes the DSP to process one complex sample is (58)*62.5 ns + 625 ns + 1.875 µs = 6.125 µs. This calculated time defines the maximum sampling rate for the demodulator and also the real-time operating window. The demodulator will fall out of real-time operation if the incoming samples arrive faster than f = 1 / 6.125 µs = 163.3 kHz. Moreover, from Equation (5.6) this sampling rate also defines the total FM signal bandwidth able to be processed by the digital FM demodulator.

5.3.2 Quantization Errors and Best-Case SNR

As mentioned in Chapter 3, the front-end A/D converter has a resolution of 8 bits. This corresponds to a theoretical 8(6 dB) = 48 dB of SNR using the 6-dB rule. Moreover, the GC1011 rounds the complex samples sent to the DSP to 16 bits, and the back-end DAC has a resolution of 12 bits. Therefore, quantization error, finite-word lengths, and rounding have an effect on the algorithm system error.

The phase estimate function coefficients were realized with 12-bit precision. This precision was chosen because it prevented overflow and the need for saturation arithmetic. Hence, there is an inherent error by quantizing the phase function coefficients to 12 bits. However, it was calculated that the relative error in the coefficients was at most 0.03%, which can be neglected as a source of significant error.

Equation (2.21) shows that after the mixing operation, a baseband FM signal has half of its original amplitude. Unfortunately, the GC1011 does not account for this "half-power" loss. Because of this fact, the GC1011 is responsible for an additional 6 dB of SNR loss before the DSP processes the data.¹ Therefore, the GC1011 effectively drops one bit of available SNR resolution, resulting in 7 bits of actual SNR resolution. Therefore, due to finite-word lengths, the best-case theoretical SNR the digital radio board can offer is 7(6 dB) = 42 dB.

¹Excerpt from a conversation with Joe Gray of Graychip, Inc.

5.4 Testing the FM Demodulator

The developed DSP code was compiled and downloaded into a boot EPROM. On system powerup, the DSP on the digital radio board uploads the boot EPROM contents, initializes the hardware, and begins execution of the demodulator software.

5.4.1 Digital Radio Software and Testing Setup

The DSP initialized the GC1011 digital receiver chip to decimate the incoming RF digital data to 50 Ksamples/sec., which corresponds to a sampling rate of 50 kHz for the DSP. This sampling rate is well within the real-time computational window of the demodulator code. The DSP also set the GC1011 tune frequency to a carrier frequency of 21.4 MHz -- a common IF output of an analog receiver. An RF signal generator was used to create a 1 kHz sine wave message signal m(t). This message mocks the synthetic signal used in the demodulator simulation. The resulting FM signal from the signal generator had a carrier frequency of 21.4 MHz, and it was used as the input to the digital radio board. The optimal amplitude for the FM input signal was determined to be -1.0 dBm through heuristic methods. By Equation (5.7), the 1 kHz sine wave message and the 50 kHz sampling rate indicates a maximum FM frequency deviation of $\Delta F = 24$ kHz. Thus, surpassing a frequency deviation of $\Delta F = 24$ kHz while testing will result in aliasing. The AM noise was unable to be fabricated in the laboratory, but the simulation proved that the algorithm works correctly with or without the presence of AM noise.

5.4.2 SNR Measurements

As discussed in the spectral analysis simulation section, a spectrum analyzer was used to measure the SNR due to harmonic distortion for the digital FM demodulator. The frequency deviation of the FM signal was stepped from $\Delta F = 1$ kHz to $\Delta F = 24$ kHz in 1 kHz increments via the RF generator. The original 1 kHz message signal was successfully demodulated by the digital radio, and the digital FM demodulator output from the onboard DAC was observed on the spectrum analyzer for purity. Depending on the frequency deviation, the worst-case SNR due to harmonic distortion was 24 dB. The best-case SNR was observed to be 36 dB. Since the spectrum analyzer output had no printing capability, the uncertainty in the SNR measurements were ± 1 dB. Table 5.1 shows the SNR figures for each increment of the frequency deviation. The table also lists the message signal strength and the largest corrupting harmonic for each SNR measurement taken.

| Frequency deviation | 1 kHz message | SNR (dB) | Largest corrupting |
|---------------------|----------------|----------|--------------------|
| $\Delta F (kHz)$ | amplitude (dB) | | harmonic |
| 1 | -8 | 32 | 3rd |
| 2 | -2 | 29 | 3rd |
| 3 | 0 | 26 | 3rd |
| 4 | 2 | 24 | 3rd |
| 5 | 4 | 24 | 3rd |
| 6 | 6 | 24 | 3rd |
| 7 | 7 | 26 | 3rd |
| 8 | 8 | 26 | 3rd |
| 9 | 9 | 27 | 3rd |
| 10 | 10 | 29 | 3rd |
| 11 | 10 | 30 | 3rd |
| 12 | 11 | 31 | 5th |
| 13 | 12 | 30 | 5th |
| 14 | 12 | 30 | 5th |
| 15 | 14 | 34 | 3rd, 5th, 7th |
| 16 | 15 | 33 | 7th |
| 17 | 16 | 34 | 7th |
| 18 | 17 | 36 | 7th |
| 19 | 17 | 34 | 7th |
| 20 | 17 | 33 | 5th |
| 21 | 17 | 32 | 5th |
| 22 | 17 | 31 | 3rd |
| 23 | 17 | 30 | 3rd |
| 24 | 17 | aliased | aliased |

Table 5.1 Frequency Deviations and FM Demodulator SNR Measurements

The test data in Table 5.1 agrees with the findings in the computer simulations. Specifically, the following observations directly correlates the test data to the simulation results.

- The major corrupting harmonics in the demodulated message were the odd harmonics.
- The range of SNR numbers in Table 5.1 is 24 dB to 36 dB. Recall, the frequency deviation of the FM signal directly effects the SNR of the demodulated message. It was shown before that the best-case SNR for the digital radio was 42 dB. Moreover, the demodulator simulation verified that there is at least a 5 dB SNR loss due to the algorithm itself. Consequently, this imposes a best-case theoretical SNR for the FM demodulator of 37 dB. The test data verifies that the demodulator never reaches the 37 dB theoretical SNR figure but comes close. The small difference from the theoretical SNR to the measured SNR can be attributed to losses inherent to the digital radio board, such as finite arithmetic and rounding errors.
- The test data also justifies the fact that the system error increases (i.e., the SNR figures decrease) by varying the FM frequency deviation. It was revealed previously that decreasing the frequency deviation below the Nyquist rate causes the statistics of the FM signal to change and thus allowing the phase vectors to reside in a high error region of the phase estimate functions.
- With a 50 kHz sampling rate, the demodulator experienced aliasing at $\Delta F = 24$ kHz. This value is consistent with the expected Nyquist rate.

The demodulator produced satisfying results using the first-order phase estimate functions. The test data concurs with the initial findings in the computer simulations. Specifically, the error in the demodulated message fluctuated significantly in some cases, but the demodulator algorithm knowingly traded accuracy for speed.

Therefore, the realization of the digital FM demodulator proved successful, and the corresponding test results demonstrated that the algorithm theory was correctly implemented and the demodulator operated up to the design expectations.

CHAPTER 6 CONCLUSION AND FUTURE DEVELOPMENT

This thesis presented the design of a digital FM demodulator as implemented on a digital radio. The concepts of digital signal processing allowed a common analog FM demodulator to be mathematically modeled and transformed into an equivalent digital version. The algorithm was first prototyped using computer simulations. These simulations verified that the algorithm integrity was preserved from theory to realization. The digital FM demodulator was then implemented with DSP software and executed in real time on the digital radio board. The FM demodulator was able to effectively demodulate narrowband FM signals. Wideband FM signals were not targeted due to the speed limitations of the digital radio board. However, the digital FM demodulator proved to be a stepping stone to other common narrowband demodulator schemes implementable on the digital radio.

Examples of several "next-step" demodulators that can be readily implemented using the digital radio and DSP techniques are listed below.

- An AM demodulator can be realized on the digital radio by simply passing the incoming complex baseband samples through a function that estimates Equation (4.2).
- A frequency-shift keying (FSK) algorithm consists of the functional blocks in Figure 4.6 without the phase angle estimate block. Since FSK only uses two modulating frequencies, the true phase angle is unnecessary.
- Multilevel signaling techniques, like quadrature-amplitude modulation (QAM) can be realized by adding the AM demodulator listed above to the block diagram shown in Figure 4.6.

The FM demodulator designed in this paper can be modified to improve its overall performance. Development of a more accurate phase angle estimator is the obvious solution for improving the algorithm performance. Methods such as a Taylor series expansion for the arctangent function in Equation (4.3) or a look-up table will improve the accuracy of the phase angle estimator. However, such modifications will trade program execution speed for the improved accuracy. Consequently, this loss in speed implies a reduction in the FM signal bandwidth the digital radio can process.

The maturation of the digital radio hardware also plays a role in the software development. A faster DSP and a faster data transfer rate between the digital receiver chip and the DSP will allow a larger RF bandwidth to be processed. Hence, wideband FM modulation and other high-bandwidth communications can be targeted with a higher speed digital radio board. The digital radio will replace the conventional analog receiver when the evolution of the digital radio reaches a point where high bandwidth, multiple-channel communication schemes can be targeted and demodulated through the use of DSP code.

APPENDIX A SIMULATION OF THE POLAR DISCRIMINATOR

The following is the Mathcad 4.0 simulation session for the polar discriminator utilized in the digital FM demodulator. The session was executed on a PC Windows-based software platform.



APPENDIX B SIMULATION OF THE PHASE ANGLE ESTIMATE FUNCTIONS

The following is the Mathcad 4.0 simulation session for the phase angle estimate functions utilized in the digital FM demodulator. The session was executed on a PC Windows-based software platform.









APPENDIX C SIMULATION OF THE DIGITAL FM DEMODULATOR

The following is the Mathcad 4.0 simulation session for the final design of the digital FM demodulator. All previous Mathcad simulations were assembled to create the framework for this final simulation environment. The session was executed on a PC Windows-based software platform.












APPENDIX D DIGITAL FM DEMODULATOR SOFTWARE LISTING

ADSP-2101 DSP Assembly Code Listing (.DSP)

{ FM_DMOD4.DSP

This program FM demodulates 1 GC1011 channel (GC1011_A) using a polar discriminator to extract the FM modulated signal. Tune frequency is set to 21.4 MHz.

MODIFICATION HISTORY

| 28-Apr-93 JMS: | Program architecture came from SYSTEST6.DSP |
|----------------|---|
| 03-May-93 JMS: | Added arctan estimator to the polar discriminator so we could |
| | sample at Nyquist. |
| 06-May-93 JMS: | Attempt to optimize arctan phase estimator |

}

.MODULE/RAM/ABS=0/SEG=IntProgMem fm_dmod4;

| .INCLUDE <d:\ad2101\include\d .INCLUDE <constants.h>; .INCLUDE <ports.h>;</ports.h></constants.h></d:\ad2101\include\d | DEF2101.H>; {Get constants for 2101 mem. map} {Get constants for initializing chips} {Get ports defined for peripherals} | |
|---|--|--|
| .VAR/PM/RAM/SEG=IntProgMem | GC1000Data[56]; { Setup data for GC1000 } | |
| .VAR/PM/RAM/SEG=IntProgMem | GC 101 IData[44]; { Setup data for GC 1011 } | |
| .VAR/DM/RAM/CIRC/SEG=IntDataM | Nem quadII_coeff[2]; {coeff for atan estimator} | |
| .VAR/DM/RAM/CIRC/SEG=IntDataM | <pre>/lem OutBuf[8]; { Setup output buffer }</pre> | |
| .VAR/DM/RAM/SEG=IntDataMem sample_rate; | | |
| .VAR/DM/RAM/SEG=IntDataMem re | eal; | |
| .VAR/DM/RAM/SEG=IntDataMem in | nag; | |
| .VAR/DM/RAM/SEG=IntDataMem re | eal_old; | |
| .VAR/DM/RAM/SEG=IntDataMem in | nag_old; | |

.VAR/DM/RAM/SEG=IntDataMem quadI_coeff;

.INIT GC1000Data: <GC1000_A.dat>; { Init. PM w/GC1000 setup } .INIT GC1011Data: <GC1011FM.dat>; { Init. PM w/GC1011 setup } { .INIT quadII_coeff: H#0324, H#096C; }

{* interrupt jump vector table *}

| JUMP MAIN; nop; nop; nop; | { reset interupt } |
|-----------------------------|------------------------------|
| JUMP OUTDATA; nop; nop; nop | ; { interrupt for DACs } |
| RTI; nop; nop; nop; | { SPORT0 transmit interupt } |
| RTI; nop; nop; nop; | { SPORT0 receive interupt } |
| RTI; nop; nop; nop; | { IRQ1 interupt } |
| RTI; nop; nop; nop; | { IRQ0 interupt } |
| RTI; nop; nop; nop; | { timer interupt } |
| | |

{* Executable code: *}

MAIN: AX0=0; { initialize DM variables } DM(real)=AX0; DM(imag)=AX0; DM(real_old)=AX0; DM(imag_old)=AX0;

> AX0=H#0C90; { quadl coeff = 0.785 / 8 coeff to } DM(quadl_coeff)=AX0; { prevent overflow }

{* NOTE: quadII coeffs are 1st scaled < 1 and then / 8 to prevent overflow *}

| I0=^quadII_coeff; | |
|--|--|
| MU=1; L0=%quadII_coeff; AX0=H#0324; DM(I0,M0)=AX0; AX0=H#096C; DM(I0,M0)=AX0; | { 3.13 format for numbers > 1 } |
| AX0=0x00F9; | { set for 50kHz output rate to DAC } |
| DM(sample_rate)=AX0; | { for initial FM bandwidth } |
| AX0=0x001F; | { Setup the system control register } |
| DM(Sys_Ctrl_Reg)=AX0; | { SPORT's disabled, Boot page=0 } |
| AX0=0x35FF; | { Setup the wait states for DM space } |
| DM(Dm_Wait_Reg)=AX0; | { DWAIT3=2,DWAIT4=3, all others 7 } |
| MSTAT = 0; | { setup FRACTIONAL results for MAC} |

| IFC = B#000000111111; | {Clear out any interupts, } |
|--|---|
| ICNTL = B#00111; | { setup IRQ2,IRQ1,IRQ0 as edge trig } |
| IMASK=0; | { disable all irqs} |
| $\begin{array}{llllllllllllllllllllllllllllllllllll$ | { Set all the circular buffer } { registers to be linear } { addressing } |

{* Setup the GC1000 chip. Transfer data from program memory to the chip. *}

| M0=1; | { Setup I0 to step one by one } |
|------------------------|-------------------------------------|
| I0=GC1000; | { beginning at GC1000's Base Addr.} |
| L4=0; | |
| M4=1; | { Setup I4 to step one by one } |
| I4=^GC1000Data; | { through PM GC1000 Setup data } |
| CNTR=%GC1000Data; | { Transfer all data in PM } |
| DO SETUP1 UNTIL CE; | |
| AX0=PM(I4,M4); | { Grab value from PM and } |
| SETUP1: DM(I0,M0)=AX0; | { move it to DM } |
| | |

{* Setup the GC1011's to their default values. See the GC1011.DAT file for the default setup information. *}

| I0=GC1011A; | { Get base addr. of GC1011-A } |
|------------------------|---|
| I4=^GC1011Data; | { Get base addr. of GC1011 setup data } |
| CNTR=11; | { Transfer the 11 bytes of setup } |
| DO SETUP2 UNTIL CE; | |
| AX0=PM(I4,M4); | { data from PM (AX0 temp. holds it) } |
| SETUP2: DM(I0,M0)=AX0; | { to GC1011 } |
| 10=GC1011B | { Get base addr. of GC1011-B } |
| CNTR=11 | { Transfer the 11 bytes of setup } |
| DO SETUP3 UNTIL CE: | |
| AX0=PM(I4.M4): | { data from PM (AX0 temp, holds it) } |
| SETUP3: DM(I0,M0)=AX0; | { to GC1011 } |
| | |
| I0=GC1011C; | { Get base addr. of GC1011-C } |
| CNTR=11; | { Transfer the 11 bytes of setup } |
| DO SETUP4 UNTIL CE; | |
| AX0=PM(I4,M4); | { data from PM (AX0 temp. holds it) } |
| | |

| SETUP4: DM(I0,M0)=AX0; | { to GC1011 } |
|-------------------------|--|
| I0=GC1011D; CNTR=11; | { Get base addr. of GC1011-D } { Transfer the 11 bytes of setup } |
| DO SETUP5 UNTIL CE; | |
| AX0=PM(I4,M4); | { data from PM (AX0 temp. holds it) } |
| SETUP5: DM(I0,M0)=AX0; | { to GC1011 } |

{* setup the programmable counter to the output clock frequency rate }

| | DM(Count_Xtrset)=AX0; DM(Count_rst)=AX0; AX0=DM(sample_rate); DM(Counter)=AX0; DM(Count_Xtrclr)=AX0; | { Set XTR line on 74F525 to stop } { clocking the counter then reset it } { Get the DAC's clocking frequency } { and send it to the 74F525 } { Re-enable clocking by clearing XTR } |
|--------------------|---|---|
| | M4 = 1; I4 = ^OutBuf; L4 = %OutBuf; | { Address generator I4 will be the } { GC1011 input side of the circular } { output buffer } |
| | I5 = ^OutBuf; L5 = %OutBuf; M5 = 1; | { I5 will be DAC output side of the } { buffer. } |
| | M1 = -1; I1 = GC1011A + QOutput1; L1=0; | { M1 will decr. address values } { Get addr. of MSB of Q output data. } |
| | I7 = ^quadII_coeff; M7 = 1; L7 = %quadII_coeff; | { pointers for poly coeffs} |
| {* Loop {* Reca | to poll the GC1011s *} II: IRQ2 = interrupt for DACs *} | |
| TEST: | IMASK=B#100000; AY0=1; AX0 = DM(OutstatA); AR = AX0 AND AY0; IF NE JUMP TEST; CALL GETDATA; CALL POLAR_DISCR; JUMP TEST; | { turn on IRQ2 } { bit 0 mask } { Get status of GC1011's output reg } { If data is ready then lets get it } { keep waiting } { Go get two data words from GC1011 } { demodulate FM signal } |

| <pre>{ ======= Subroutine POLAR_DISCR ====================================</pre> | |
|--|---|
| POLAR_DISCR: AX0=DM(imag_old); AR= -AX0; MX0= AR; MY0=DM(real); | { polar discriminator multiples new } { sample x conjugate(old sample) } { get conjugate of old imag part } |
| MR=MX0 * MY0 (SS); MX0=DM(imag); MY0=DM(real_old); | { 1st Im term in a complex multiply } |
| MR=MR + MX0 * MY0 (SS); AX1=MR1; | { IMAGINARY term of complex multiply } { temp storage for Im term } |
| MX0=DM(real); MR=MX0 * MY0 (SS): | { 1st real term } |
| MX0=DM(imag); MX0=DM(imag, old); | { 2nd real term} |
| MR=MR + MX0 * MY0 (SS); AY0=MR1; | { REAL term of complex multiply} { temp storage for Re term } |
| AR=PASS MR1; IF GE JUMP QUADI_EST; | { see if in quadrant I or IV } |

{* Phase approximation for quadrant II takes the form of Lagrange *} {* interpolating poly y = -.785398 * x + 2.356194 *}

| QUADII_EST: AR=ABS AX1; | { if Im component is '-', move to quad II } |
|----------------------------|---|
| AR=AR+AY0; | { numerator of ratio = Im + Re } |
| AY1=AR; | { prep for division, dividend in AY1, AY0 } |
| AR=ABS AX1; | |
| AR=AR-AY0; | { denominator of ratio = Im - Re } |
| AX0=AR; | { prep for division, divisor in AX0 } |
| AY0=0; | { lower half of numerator is 0 } |
| CALL DIVISION; | |
| MX0=AY0; | { get result of division for poly approx. } |
| MY0=DM(I7,M7); | { multiply it by 1st coeff } |
| MR=MX0 * MY0 (SS), AY0=DM(| [17,M7) ; |
| AR=-MR1; | |
| AR=AR + AY0; | { add to result } |
| SR=ASHIFT AR BY 2 (LO); | { shift 3.13 back into 1.15 format } |

AR=SR0; { check Im result to see if quad II or III } AF=PASS AX1; { if Im is in quad 3, negate phase answer } IF LT AR=-SR0; JUMP PHASE_EST; {* Phase approximation for guadrant I takes the form of Lagrange *} {* interpolating poly y = -0.785398 * x + 0.785398 *} QUADI_EST: AF=ABS AX1; { if Im part is '-', put in quad I } AR=MR1-AF; { numerator for ratio = Re - Im } AY1=AR: { prep for division, dividend in AY1 } AX0=AY0; { move Re component } AR=AX0+AF; { denominator is Re + Im } AX0=AR; { divisor is in AX0 } AY0=0; CALL DIVISION; MX0=AY0; MY0=DM(quadI_coeff); MR=MX0 * MY0 (SS), AY0=MY0; AR=-MR1; AR=AR + AY0; { add to result } { check Im result to see if guad I or IV } AF=PASS AX1; IF LT AR=-AR; { if in guad 4, negate phase answer }

PHASE_EST: SR=ASHIFT AR BY 1 (LO); DM(I4,M4)=SR0; { add max gain to prevent DAC overflow } { store phase result to out buffer}

{* Store current sample as old sample for next discriminator calculation }

| AX0=DM(real); | { get current real part } |
|-------------------|--------------------------------|
| DM(real_old)=AX0; | |
| AX0=DM(imag); | { get current imaginary part } |
| DM(imag_old)=AX0; | |

RTS;

DIVISION: DIVS AY1,AX0;

DIVQ AX0; RTS; * This subroutine will read the imaginary and real data value from the
* GC1011. The routine reads the MSB of the Q-value, shifts it and then
* concatenates the LSB. The same thing is done with the real value.
* the results are stored using address in I4.
* Registers Used.....
I1 = Address where MSB Q value for the GC1011 is M1 = -1, so address is decremented to get Q and I values from GC1011 I4 = Address where results are stored. M4 = Increment I4's address by one.

AX0, AX1, AY0, AF, AR, SR are used in computation. }

| { Get the MSByte from GC1011 and } { move this to MSB of 16 bit value } { Get the LSByte and clear the MSByte } { Value to zero out MSB's } { to zero. Append this to GC1011's } { MSByte to form 16 bit word } { Temp. store Q results in AX1 } |
|--|
| { Get the MSByte from GC1011 and } { move this to MSB of 16 bit value } { Get the LSByte and clear the MSByte } { to zero. Append this to GC1011's } { MSByte to form 16 bit word } |
| { Store real value first (I reg.) } { Store imaginary (Q reg.) } |
| { Reset addr. of GC1011's Q output. } { Reset the value of AY0 } { Get GC1011's status and } { set the data ready bit. } { Send this back to the GC1011 } { and go back to work } |
| |

- * This service routine will take a data value from a buffer and output it to
- * DAC1.

* Registers Used.....

I5 = Address where results are stored. M5 = Increment I5's address by one. SI = Temporary holding register. }

OUTDATA: ENA SEC_REG;

SI = DM(I5,M5); SR = LSHIFT SI BY -4 (LO); AY1 = H#0800; AR = SR0 XOR AY1; DM(DAC_1) = AR;

DIS SEC_REG; RTI;

.ENDMOD;

{ Complete the module }

{ enable secondary registers to} { preserve registers before IRQ} { Get value to send to DAC }

{ Convert 16 bit value to 12 bit } { Convert this 2's complement word }

{ to offset binary for DAC }

ADSP-2101 System Builder File (.SYS)

.SYSTEM fm_dmod4; .ADSP2101; .MMAP0;

.SEG/PM/RAM/ABS=0x0000/CODE/DATA IntProgMem[2048]; .SEG/PM/RAM/ABS=0x0800/CODE/DATA ExtProgMem[14336];

.SEG/DM/RAM/ABS=0x0000 ExtDataMem[12288]; .SEG/DM/RAM/ABS=0x03800 IntDataMem[1024];

.SEG/ROM/BOOT=0 boot_mem[2048];

{* ports for the memory-mapped peripherals in the DM map *}

.PORT/DM/ABS=0x03280 Counter; .PORT/DM/ABS=0x03300 DAC_1; .PORT/DM/ABS=0x03301 DAC_2; .PORT/DM/ABS=0x03380 DAC_3; .PORT/DM/ABS=0x03381 DAC_4;

{ specific ports for the DUART }

.PORT/DM/ABS=0x03400 Mode_regA; .PORT/DM/ABS=0x03401 Status_clk_regA; .PORT/DM/ABS=0x03402 ISR_Cmd_regA; .PORT/DM/ABS=0x03403 Data_regA; .PORT/DM/ABS=0x03404 IPCR_ACR_reg; .PORT/DM/ABS=0x03405 ISR2_IMR_reg; .PORT/DM/ABS=0x03408 Mode_regB; .PORT/DM/ABS=0x03408 Mode_regB; .PORT/DM/ABS=0x03408 Data_regB; .PORT/DM/ABS=0x0340B Data_regB; .PORT/DM/ABS=0x0340C IVR_reg; .PORT/DM/ABS=0x0340C IVR_reg; .PORT/DM/ABS=0x0340E Go_cnt_set_out; .PORT/DM/ABS=0x0340F Stop_cnt_clr_out; { specific ports for the 4 GC1011 receiver chips }

{GC1011A chip}

.PORT/DM/ABS=0x0308F Qout1A; .PORT/DM/ABS=0x0308E Qout0A; .PORT/DM/ABS=0x0308D lout1A; .PORT/DM/ABS=0x0308C lout0A; .PORT/DM/ABS=0x0308A OutstatA;

{GC1011B chip}

.PORT/DM/ABS=0x0310F Qout1B; .PORT/DM/ABS=0x0310E Qout0B; .PORT/DM/ABS=0x0310D lout1B; .PORT/DM/ABS=0x0310C lout0B; .PORT/DM/ABS=0x0310A OutstatB;

{GC1011C chip}

.PORT/DM/ABS=0x0318F Qout1C; .PORT/DM/ABS=0x0318E Qout0C; .PORT/DM/ABS=0x0318D lout1C; .PORT/DM/ABS=0x0318C lout0C; .PORT/DM/ABS=0x0318A OutstatC;

{GC1011D chip }

.PORT/DM/ABS=0x0320F Qout1D; .PORT/DM/ABS=0x0320E Qout0D; .PORT/DM/ABS=0x0320D lout1D; .PORT/DM/ABS=0x0320C lout0D; .PORT/DM/ABS=0x0320A OutstatD;

{ ports to control the counter }

.PORT/DM/ABS=0x03289 Count_rst; .PORT/DM/ABS=0x03291 Count_Xtrset; .PORT/DM/ABS=0x03299 Count_Xtrclr;

.ENDSYS;

REFERENCES

| [Ana90] | Analog Devices, ADSP-2101 User's Manual, 1st Edition. Analog Devices, Norwood, MA, February 1990. |
|---------|--|
| [Cou90] | Couch, Leon W. <u>Digital and Analog Communication Systems, 3rd Edition</u> . Macmillan Publishing Company, New York, 1990. |
| [Gra91] | Graychip, GC1011 Digital Receiver Chip Data Sheet. Graychip, Inc., Palo Alto, CA, May 1991. |
| [Hag88] | Hager, William W. <u>Applied Numerical Linear Algebra</u> . Prentice Hall, Englewood Cliffs, NJ, 1988. |
| [Mit93] | Mitra, Sanjit, & Kaiser, James. <u>Handbook for Digital Signal Processing</u> . John Wiley & Sons, New York, 1993. |
| [Opp89] | Oppenheim, Alan, & Schafer, Ronald. <u>Discrete-Time Signal Processing</u> . Prentice Hall, Englewood Cliffs, NJ, 1989. |
| [Str88] | Strum, Robert, & Kirk, Donald. <u>Discrete Systems and Digital Signal</u> <u>Processing</u> . Addison-Wesley Publishing Company, Reading, MA, 1988. |

BIOGRAPHICAL SKETCH

The author was born in Cleveland, Ohio, on February 4, 1969. He received his Bachelor of Science in Electrical Engineering degree in December of 1992 from the University of Florida. He returned to the University of Florida in August of 1993 to pursue a master's degree in electrical engineering. He is scheduled to receive a Master of Science degree in May of 1995.

Throughout his undergraduate and graduate career, the author completed five cooperative education tours with the Central Intelligence Agency in Langley, Virginia, where he was exposed to digital communications and DSP applications. During his graduate program, he also worked as a graduate teaching assistant for the Digital Design Lab.

He will be pursuing a career in DSP applied research in the private or government sector following graduation.

I certify that I have read this study and that in my opinion it conforms to acceptable standards of scholarly presentation and is fully adequate, in scope and quality, as a thesis for the degree of Master of Science.

> Scott L. Miller, Chairman Associate Professor of Electrical Engineering

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Jose C. Principe, Co-chairman Professor of Electrical Engineering

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> Michel A. Lynch Lecturer of Electrical Engineering

This thesis was submitted to the Graduate Faculty of the College of Engineering and to the Graduate School and was accepted as partial fulfillment of the requirements for the degree of Master of Science.

May 1995

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Dean, Graduate School